# Grap - A Language for Typesetting Graphs Tutorial and User Manual 

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ABSTRACT

Grap is a language for describing plots of data. This graph of the 1984 age distribution in the United States

is produced by the grap commands
(Each line in the data file agepop. d contains an age and the number of Americans of that age alive in 1984; the file is sorted by age.)

The grap preprocessor works with pic)pic $\mid$ reference(latest and trofftroff $\mid$ reference(latest Most of its input is passed through untouched, but statements between .G1 and .G2 are translated into pic commands that draw graphs.

## 1. Introduction

Grap is a language for describing graphical displays of data. It provides such services as automatic scaling and labeling of axes, and for statements, if statements, and macros to facilitate user programmability. Grap is intended primarily for including graphs in documents prepared on the UNIX® operating system, and is only marginally useful for elementary tasks in data analysis.

Section 2 of this document is a tutorial introduction to grap; readers who find it slow going may wish to skim ahead. The examples in Section 3 illustrate the various kinds of graphs that grap can produce and some common grap idioms. Mundane matters about using grap are discussed in Section 4, and Section 5 contains a brief reference manual.

We have tried to illustrate good principles of statistics and graphical design in the graphs we present. In several places, though, good taste has lost to the necessity of illustrating grap capabilities. Readers interested in statistical integrity and taste should consult the literature, for example $\mid$ reference(chambers graphs) $\mid$ reference(tufte graphs) $\mid$ reference(cleveland elements).

## 2. Tutorial

The following is a simple grap program $\dagger$

```
.G1
54.2
49.4
49.2
50.0
48.2
43.87
. G2
```

The single number on each line is the winning time in seconds for the men's 400 meter run, from the first modern Olympic Games (1896) to the twenty-first (1988). If the file olymp.g contains the text above, then typing the command

```
grap olymp.g | pic | troff > junk
```

creates a troff output file junk that contains the picture


The graph shows the decrease in winning times from 54.2 seconds to 43.87 seconds. If the times are contained in the file 400 mt imes. d , we could produce the same graph with the shorter program

Writing copy "fname" in a grap program is equivalent to including the contents of file fname at that point in the file. (In the interests of compatibility with other programs, include is a synonym for copy.)

Each line in the file 400 mpairs . d contains two numbers, the year of the Olympics and the winning time:

[^0]```
1896 54.2
1900 49.4
1904 49.2
1908 50.0
191248.2
198843.87
```

If we plot this data with the program
the bottom $(x)$ axis represents the year of the Olympics.


The 'holes" in $x$-values reflect the fact that the 1916, 1940, and 1944 Olympics were cancelled due to war. Because the previous data (in 400 mt imes.d) had just one number per line, grap viewed it as a 'time series'" and supplied $x$-values of $1,2,3, \cdots$ before plotting the data as $y$-values. The input to the second program has two values per line, so they are interpreted as $(x, y)$ pairs.

Rather than a scatter plot of points, we might prefer to see the winning times connected by a solid line. The program
produces the graph


Eric Liddell of Great Britain won his gold medal in Paris in 1924 with a time of 47.6 seconds. (Remember "Chariots of Fire'’?)

We can make the graph more attractive by modifying its frame and adding labels.

The frame command describes the graph's bounding box: the overall frame (which has four sides) is invisible, it is 2 inches high and 3 inches wide (which happen to be the default height and width), and the left and bottom sides are solid (they could have been dashed or dotted instead). The labels appear on the left and bottom, as requested.


To set the range of each axis, grap examines the data and pads both dimensions by seven percent at each end. The coord ('coordinates') command allows you to specify the range of one or both axes explicitly; it also turns off automatic padding.

The $y$-axis now ranges from 42 to 56 seconds (a little more than before), and the $x$-axis from 1894 to 1990 (a little less).


The ticks in the preceding graphs were generated by grap guessing at reasonable values. If you would rather provide your own, you may use the ticks command, which comes in the flavors illustrated below.

The first ticks command deals with the left axis: it puts the ticks facing out at the numbers in the list. Grap puts labels only at values with strings, except that when no labels at all are given, each number serves as its own label, as in the second ticks command. That command is for the bottom axis: it puts the ticks facing in at steps of 20 from 1900 to 1980. The command ticks off turns off all ticks. Grap does its best to place labels appropriately, but it sometimes needs your help: the left . 2 clause moves the left label 0.2 inches further left to avoid the new ticks.


The file 400 wpairs.d contains the times for the women's 400 meter race, which has been run only since 1964.

| 1964 | 52 |
| :--- | :--- |
| 1968 | 52 |
| 1972 | 51.08 |
| 1976 | 49.29 |
| 1980 | 48.88 |
| $\ldots$ |  |
| 1988 | 48.65 |

To add these times to the graph, we use
The new command tells grap to end the old curve and to start a new curve (which in this case will be drawn with a dotted line). Text is placed on the graph by commands of the form
"string" at xvalue, yvalue
The size clauses following the quoted strings tell grap to shrink the characters by three points (absolute point sizes may also be specified). Strings are usually centered at the specified position, but can be adjusted by clauses to be illustrated shortly.


The file phone. d records the number of telephones in the United States from 1900 to 1970.

```
00 1.3
01 1.8
02 2.3
03 2.8
043.3
...
70 120.2
```

Each line gives a year and the number of telephones present in that year (in millions, truncated to the nearest hundred thousand). The simple grap program
produces the simple graph


The number of telephones appears to grow exponentially; to study that we will plot the data with a logarithmic $y$-axis by adding log y to the coord command. We will also add cosmetic changes of labels, more ticks, and a solid line to replace the unconnected dots.

The third ticks command provides a string that is used to print the tick labels. C programmers will recognize it as a print $f$ format string; others may view the $\% g$ as the place to put the number and anything else (in this case just an apostrophe) as literal text to appear in the labels. To suppress labels, use the empty format string (""). The program produces


The number of telephones grew rapidly in the first decade of this century, and then settled down to an exponential growth rate upset only by a decrease in the Great Depression and a post-war growth spurt to return the curve to its
pre-Depression line.
Our presentation so far has been to start with a simple grap program that illustrates the data, and then refine it. Later in this document we will ignore the design phase, and present rather complex graphs in their final form. Beware.

All the examples so far have placed data on the graph implicitly by copying a file of numbers (either a time series with one number per line or pairs of numbers). It is also possible to draw points and lines explicitly. The grap commands to draw on a graph are illustrated in the following fragment.

The grid command is similar to the ticks command, except that grid lines extend across the frame. The next few commands plot text at specified positions. The plotting characters (such as bullet) are implemented as predefined macros - more on that shortly. Unlike arbitrary characters, the visual centers of the markers are near their plotting centers. The circle command draws a circle centered at the specified location. A radius in inches may be specified; if no radius is given, then the circle will be the small circle shown at the center of the graph. The line and arrow commands draw the obvious objects shown at the upper left.


This figure also illustrates the combined use of the draw and next commands. Saying draw A solid defines the style for a connected sequence of line fragments to be called A. Subsequent commands of next A at point add point to the end of A. There are two such sequences active in the above example (A and B); note that their next commands are intermixed. Because the predefined string delta follows the specification of $B$, that string is plotted at each point in the sequence.

Grap has numeric variables (implemented as double-precision floating point numbers) and the usual collection of arithmetic operators and mathematical functions; see the reference section for details.

Grap provides the same rudimentary macro facility that pic does:

```
define name { replacement text }
```

defines name to be the replacement text. The replacement may be any text that contains balanced open and closing braces \{ \}. (Alternatively, the replacement text may be quoted by any single character that does not appear in the replacement; the string is terminated by the next occurrence of that character.) Any subsequent occurrence of name will be replaced by replacement text.

The replacement text of a macro definition may contain occurrences of $\$ 1, \$ 2$, etc.; these will be replaced by the corresponding actual arguments when the macro is invoked. The invocation for a macro with arguments is

```
name(arg1, arg2, ...)
```

Non-existent arguments are replaced by null strings.
The following grap program uses macros and arithmetic to plot crude approximations to the square and square root functions.

The macro root uses the ${ }^{\wedge}$ exponentiation operator. (Because grap has the square root function sqrt, that macro
is in fact superfluous.) The program produces


The copy command has a thru parameter that allows each line of a file to be treated as though it were a macro call, with the first field serving as the first argument, and so on. This is the typical grap mechanism for plotting files that are not stored as time series or as $(x, y)$ pairs. We will illustrate its use on the file states.d, which contains data on the fifty states.

| AK | 1 | 401851 |
| :--- | :--- | :--- |
| WY | 1 | 469557 |
| VT | 1 | 511456 |
| DE | 1 | 594338 |
| ND | 1 | 652717 |
| M |  |  |
| CA | 45 | 23667902 |

The first field is the postal abbreviation of the state's name (Alaska, Wyoming, Vermont, ...), the second field is the number of Representatives to Congress from the state after the 1981 reapportionment, and the third field is the population of the state as measured in the 1980 Census. The states appear in increasing order of population.

We will first plot this data as population, representative pairs. (In the coord statement, log log is a synonym for $\log x \log y$.)

Although the population is given in persons, the Plot St ate macro plots the population in millions by dividing the third input field by one million (written in exponential notation as $1 e 6$, for $1 \times 10^{6}$ ).


Using circle as a plotting symbol displays overlapping points that are obscured when the data is plotted with bullets. The representation of a state is roughly proportional to its population, except in the very small states.

Our next plot will use the state's rank in population as the $x$-coordinate and two different $y$-coordinates: population and number of representatives. We will use two coord commands to define the two coordinate systems pop and rep. We then explicitly give the coordinate system whenever we refer to a point, both in constructing axes and plotting data.

The copy statement in the program uses an immediate macro enclosed in curly brackets and thus avoids having to name a macro for this task. Because the program assumes that the states are sorted in increasing order of population, it generates thisrank internally as a grap variable. The program produces


The plotting symbols were chosen for contrast in both shape and shading. This graph also indicates that representation is proportional to population. Once we see this graph, though, we should realize that we don't really need two coordinate systems: we can relate the two by dividing the population of the U.S. - about 226,000,000 - by the number of representatives - 435 - to see that each representative should count as 520,000 people. If the purpose of this graph were to tell a story about American politics rather than to illustrate multiple coordinate systems, it should be redrawn with a single coordinate system.

Many graphs plot both observed data and a function that (theoretically) describes the data. There are many ways to draw a function in grap: a series of next commands is tedious but works, as does writing a simple program to write a data file that is subsequently read and plotted by grap. The for statement often provides a better solution. This grap program
produces


The for statement uses the same syntax as the ticks statement, but the from keyword can be replaced by " $=$ '",
which will look more familiar to programmers. It varies the index variable over the specified range and for each value executes all statements inside the delimiter characters, which use the same rules as macro delimiters. It is, of course, useful for many tasks beyond plotting functions.

The if statement provides a simple mechanism for conditional execution. If a file contains data on both cities and states (and lines describing states have " $S$ '' in the first field), it could be plotted by statements like

```
if "$1" == "S" then {
    PlotState($2,$3,$4)
} else {
    PlotCity($2,$3,$4,$5,$6)
}
```

The else clause is optional; delimiters use the same rules as macros and for statements.

## 3. A Collection of Examples

The previous section covered the grap commands that are used in common graphs. In this section we'll spend less time on language features, and survey a wider variety of graphs. These examples are intended more for browsing and reference than for straight-through reading. Be prepared to refer to the manual in Section 5 when you stumble over a new grap feature.

The file cars. d contains the mileage (miles per gallon) and the weight (pounds) for 74 models of automobiles sold in the United States in the 1979 model year.

| 22 | 2930 |
| :---: | :---: |
| 17 | 3350 |
| 22 | 2640 |
| 17 | 2830 |
| 23 | 2070 |
| $\cdots$ |  |
| 17 | 3170 |

The trivial grap program
produces


This graph shows that weights bottom out somewhat below 2000 pounds and that heavier cars get worse mileage; it is hard to say much more about the relationship between weight and mileage.

The next graph provides labels, uses circles to expose data hidden in the clouds of bullets, and re-expresses the $x$-axis in gallons per mile. It also changes the point size and vertical spacing to a size appropriate for camera-ready journal articles and books; the size changes should be made outside the grap program. The .ft command changes to a Helvetica font, which some people prefer for graphs.

Grap supports logarithmic re-expression of data with the log clause in the coord statement; any other reexpression of data must be done with grap arithmetic, as above.


This graph shows that gallons per mile is roughly proportional to weight. (The two outliers near 4000 pounds are the Cadillac Seville and the Oldsmobile 98.)

In Visual Display of Quantitative Information, Tufte proposes the 'dot-dash-plot'" as a means for maximizing data ink (showing the two-dimensional distribution and the two one-dimensional marginal distributions) while minimizing what he calls 'chart junk' - ink wasted on borders and non-data labels. His preference is easy to express in grap:

Although visually attractive, we do not find the resulting graph as useful for interpreting the data.


Tufte's graph does point out two facts that are not obvious in the previous graphs: there is a gap in car weights near 3000 pounds (exhibited by the hole in the $y$-axis ticks), and the gallons per mile axis is regularly structured (the ticks
are the reciprocals of an almost dense sequence of integers). The reader may decide whether those insights are worth the decrease in clarity.

Throughout the twentieth century, horses, cars and people have gotten faster; let's study those improvements. For horses, we'll consider the winning times of the Kentucky Derby from 1909 to 1988, in the file speedhorse.d:
126.2
126.4
125.0
129.4
124.8
...
122.2

The program
produces the graph


Each race is recorded with a bullet and record times are marked by horizontal lines. Secretariat is the only horse to have run the one-and-a-quarter-mile race in under two minutes; he won in 1973 in 1:59.4.

For automobiles we will study the world land speed record (even though those vehicles are by now just lowflying airplanes). The file speedcar.d lists years in which speed records were set and the record set in that year, in miles per hour averaged over a one-mile course.

| 06 | 127 |
| :--- | :--- |
| 10 | 131 |
| 11 | 141 |
| 19 | 149 |
| 20 | 155 |
| $\ldots$ |  |
| 83 | 633 |

We will plot the data with the following grap program, which uses nested braces in the copy and if statements.

Each record line is drawn after the next record is read, because the program must know when the record was broken to draw its line. The if statement handles the first record, and the extra line command extends the last record out to the current date.


The horizontal lines reflect the nature of world records: they last until they are broken. The records could also have been plotted by a scatterplot in which each point represents the setting of a record, but it would be misleading to connect adjacent points with line segments (which we inappropriately did in the graphs of the Olympic 400 meter run).

The following graph shows the world record times for the one mile run; because its grap program is so similar to its automotive counterpart, we won't show the program or data.


The three graphs show three different kinds of changes. Although horses are getting faster, they appear to be approaching a barrier near two minutes. Cars show great jumps as new technologies are introduced followed by a plateau as limits of the technology are reached. Milers have shown a fairly consistent linear improvement over this century, but there must be an asymptote down there somewhere.

The next file gives the median heights of boys in the United States aged 2 to 18 , together with the fifth and ninety-fifth percentiles.

```
2 82.5 86.8 94.4
3 89.0 94.9 102.0
95.8 102.9 109.9
102.0 109.9 117.0
107.7 116.1 123.5
18 165.7 176.8 187.6
```

The heights are given in centimeters ( 1 foot $=30.48$ centimeters ). The trivial program
displays the data as


Because there are four numbers on each input line, the first is taken as an $x$-value and the remaining three are plotted as $y$-values.

The three curves appear to be roughly straight (at least up to age 16), so it makes sense to fit a line through them. We will use the standard least squares regression in which

$$
\text { slope }=\frac{n \Sigma x y-\Sigma x \Sigma y}{n \Sigma x^{2}-(\Sigma x)^{2}}
$$

(where the summations range over all $n x$ and $y$ values in the data set) and the $y$-intercept is

$$
\frac{\Sigma y-\text { slope } \times \Sigma x}{n}
$$

The following grap program boldly (and rather foolishly) implements that formula.
It plots the extreme fifth percentiles as a bar through the median, which is plotted as a bullet. All heights are converted to feet before plotting and calculating the regression line.


Grap print statements write on stderr as they are processed by grap; their single argument can be either an expression or a string. The print statements (which are commented out in the above grap program) at one time showed that the regression line is

$$
\text { Height in Feet }=2.61+.19 \times \text { Age }
$$

Thus for most American boys between 3 and 16, you may safely assume that they started out life at 2 feet 7 inches and grew at the rate of two and a quarter inches per year.

This program probably misapplies grap; if you really want to perform least squares regressions on data, you should usually use a simple $a w k$ program like
(Be warned, though, that this program is not numerically robust.)
While we're on the subject of fitting straight lines to data, we'll redraw three graphs from J. W. Tukey's Exploratory Data Analysis. The file usapop. d records the population of the United States in millions at ten-year intervals.

| 1790 | 3.93 |
| :--- | ---: |
| 1800 | 5.31 |
| 1810 | 7.24 |
| 1820 | 9.64 |
| 1830 | 12.87 |
| $\ldots$ |  |
| 1950 | 150.7 |

Tukey's first two graphs indicate that the later population growth was linear while the early growth was exponential. The following grap program plots them as a pair, using graph commands to place internally unrelated graphs adjacent to one another.

The statements defining each graph are indented for clarity. The second graph has the northern point of its frame 0.05 inch below the southern point of the frame of the first graph; the with clause is passed directly through to pic without being evaluated for macros or expressions. The names of both graphs begin with capital letters to conform to pic syntax for labels.


Linear Scale, Linear Fit

Logarithmic Scale, Exponential Fit

Polynomial functions lie between the linear and exponential functions; Tukey shows how a seventh-degree polynomial provides a better (and longer) fit to the early population growth.

This program re-expresses the $x$-axis with grap arithmetic and uses an if statement to graph only part of the data file. It produces


The eqn space 0 clause is necessary to keep eqn from adding extra space that would interfere with positions computed by grap; see Section 4.

The file army. d contains four related time series describing the United States Army.

| 40 | 16 | .9 | 249 | 1 |
| ---: | ---: | ---: | ---: | ---: |
| 42 | 190 | 12 | 2867 | 1 |
| 43 | 521 | 36 | 6358 | 55 |
| 44 | 692 | 47 | 7144 | 71 |
| 45 | 772 | 62 | 7283 | 90 |
| $\cdots$ |  |  |  |  |
| 83 | 80 | 9 | 606 | 67 |

The first field is the year; the next four fields give the number of male officers, female officers, enlisted males and enlisted females, each in thousands. (Actually, there were no female enlisted personnel in the Army until 1943; the value 1 in 1940 and 1942 is just a placeholder, since grap has no mechanism for handling missing data.) The following grap program draws the four series with four different sets of draw and next commands.

The program labels the lines by copying immediate data; the program is therefore shorter to write and easier to change. The delimiter string XXX in the until clause could be deleted in this graph: the . G2 line also denotes the end of data. Even though that string is enclosed in quotes, it may not contain spaces. The $y$-positions of the labels are the result of several iterations.


This data can tell many stories: the buildup during the Second World War is obvious, as is the exodus after the war; increases during Korea and Vietnam are also apparent. We will consider a different story: the ratio of enlisted men to the three other classes of personnel. There are several ways to plot this data (the most obvious graph uses three time series showing how the ratios change over time, and is left as an exercise for the reader).

We will instead construct a graph that gives little insight into this data, but illustrates a general method that is quite useful in conjunction with grap. The graph is a 'scatterplot vector'" that shows how one variable (the number of enlisted men) varies as a function of the other three. Breaking with tradition, we first show the final graphs, all of which have logarithmic scales.


The number of enlisted men is almost linearly related to the number of male officers, it is somewhat related to the number of female officers, and it varies widely as a function of the number of enlisted women.

Much more interesting than the graph itself is the method we used to produce it. We wrote a miniature "compiler'" that accepts as its "source language" a description of a scatterplot vector and produces as 'object code" a grap program to draw the graph. The source program for the above example is

The program lists several global attributes of the graph, the $y$-variable to be plotted, and as many $x$-variables as are desired; with each variable is its field in the file and a descriptive string. The language is 'compiled' by the following awk program.

Running this program on the above description produces the following output, which is typically piped directly to grap.

The generated program uses the pic trick of re-using the same name (A) for several objects.

Although the program above is merely a toy, 'minicompilers', can produce useful preprocessors for grap. The scatmat program, for instance, is a 90 -line $a w k$ program that reads a simple input language and produces as output a grap program to produce a "scatterplot matrix", which is a handy graphical device for spotting pairwise interactions among several variables. If grap lacks a feature you desire, consider building a simple preprocessor to provide it. An alternative is to define macros for the task; which approach is best depends strongly on the job you wish to accomplish.

The next graph uses iterators to make a graph without reading data from a file. Rather, its "data" is a function of two variables that describes a derivative field and a function of one variable that describes one solution to the differential equation.

The left label uses eqn text between the $\$ \$$ delimiters. The variable scale ensures that all lines in the direction field are the same length. The in clauses in the ticks statements specify that the ticks go in zero inches to avoid overprinting. The variables $t x$ and $t y$ are so named because $x$ and $y$ are reserved words for the coord statement.


Programmers familiar with floating point arithmetic may be surprised that the above graph is correct. Because of roundoff error, iteration 'from 0 to 1 by . 05 '' usually produces the values $0, .05, .10, \ldots, .95$. Grap uses a "fuzzy test'" in the for statement to avoid that problem, which may in turn introduce other problems. Such problems may be avoided by iterating over an integer range and incrementing a non-integer value within the loop.

Most of the data we have seen so far is inherently two (or more) dimensional. As an example of onedimensional data, we will return to the populations of the fifty states, which is the third field in the file states.d introduced earlier; the file is sorted in increasing order of population. Our first graph takes the most space, but it also gives the most information.

The L macro (for Label) with input parameter $X$ evaluates to the number $2^{X} / 1,000,000$ followed by the string " $X$ " (the ticks command expects a number followed by a string label).


The dotted line is the least squares regression

$$
\log _{10} \text { Population }=7.214-.03 \times \text { Rank }
$$

which gives 15.3 million as the population of the largest state and .515 million as the population of the smallest state. It says that population drops by a factor of two every ten states (compare the top and left scales). As sloppy as the exponential fit is, though, it is a much better fit to this data than a Zipf's Law curve is (drawing that curve is left as an exercise for the reader).

The next graph is a more standard representation of one-dimensional data.
The markers were chosen to be vticks because they denote only an $x$-value.


The next one-dimensional graph uses the state's name as its marker; to reduce overprinting the graph is 'jittered'" by using a random number as a $y$-value.

The function rand () returns a pseudo-random real number chosen uniformly over the interval $[0,1)$.


This graph is too cluttered; circles would have been a better choice as a plotting symbol (bullets, once again, would hide data).

Histograms are a standard way of presenting one-dimensional data in two-dimensional form. Our first step in building a histogram of the population data is the following awk program, which counts how many states are in each 'bin'" of a million people.

The variable bzs tells where bin zero starts; although it is zero in this graph, it might be 95 in a histogram of human body temperatures in degrees Fahrenheit. The program produces the following output in states $2 . \mathrm{d}$ :
$0 \quad 12$
15
27
35
47
231
There are 12 states with population between 0 and $999,999,5$ states with population between $1,000,000$ and $1,999,999$, and so on.

This grap program uses three line commands to plot each rectangle in the histogram.
It produces


The same file can be plotted in a more attractive (and more useful) form by
which produces one of Bill Cleveland's 'dot charts'" or 'lolliplots'":

(We use $\backslash$ (bu, the troff character for a bullet, rather than the built-in string to get a larger size.)
Other histograms are possible. The following $a w k$ program
produces the file states3.d

```
AK O O
WY O 1
VT O 2
DE O 3
ND 0 4
CA 23 0
```

which lists the state's abbreviation, bin number, and height within the bin. The grap program
reads that file to make the following histogram, in which the state names are used to display the heights of the bins. In each bin, the states occur in increasing order of population from bottom to top.

```
HI
RI
ID
NH
NV
mT IA mO
SD CO WI
ND WV AZ AL TN NC
DE NE OR KY MD MA
vt UT MS SC LA IN
WY NM KS CT WA GA FL PA
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multicolumn{2}{|r|}{AK ME AR OK MN V} & NJ & MI OH IL & TX & NY & CA \\
\hline &  & &  & 1 & 1 & \\
\hline 0 & 5 & & 10 & 15 & 20 & 25 \\
\hline
\end{tabular}
```

The next data set is a run-time profile of an early version of grap, created by compiling the program with the -p option and running prof after the program executed.

| \%time | cumsecs | \#call | ms/call | name |
| ---: | ---: | ---: | ---: | :--- |
| 21.1 | 11.02 | 26834 | 0.41 | -yylook |
| 11.2 | 16.89 | 30 | 195.60 | _yyparse |
| 9.3 | 21.75 |  |  | _doprnt |
| 9.1 | 26.52 |  |  | -write |
| $\ldots$ |  |  |  |  |
| 0.0 | 52.19 | 170 | 0.00 | _tickside |

Although there were more than fifty procedures in the program, the top four time-hogs accounted for more than half of the run time. This file is difficult for grap to deal with: even though if statements would allow us to extract lines 2 through 11 of the file, we could not remove the leading _ from a routine name or access the last field in a record. We will therefore process it with the following awk program.

The program produces

```
21.1 yylook
11.2 yyparse
9.3 _doprnt
9.1 write
5.9 input
...
2.0 nextchar
```

We could even use the sh statement to execute the $a w k$ program from within grap, which would make the latter entirely self-contained (see the reference manual for details).

We will display the data with this program.
Observe that the program knows nothing about the range of the data. It uses default ticks and a frame statement with a computed height to achieve total data independence.


This bar chart highlights the fact that most of the time spent by grap is devoted to input and output.
J. W. Tukey's box and whisker plots represent the median, quartiles, and extremes of a one-dimensional distribution. The following grap program defines a macro to draw a box plot, and then uses that shape to compare the distribution of heights of volcanoes with the distribution of heights of States of the Union.

Boxes are one of many shapes used for the graphical representation of several quantities. If you use such shapes frequently then you should make a library file of their macros to copy into your grap programs. The above program produces


Even though the extreme heights are the same, state heights have a lower median and a greater spread.
Someday you may use grap to prepare overhead transparencies, only to find that everything comes out too small. The following program illustrates some ways to get larger graphs.

The ps and vs commands preceding the graph set the text size to 14 points and the vertical spacing to 18 points; the two quantities are reset by the commands following the .G2. Such size changes should be made outside the grap program, as mentioned earlier. The 4 following the .G1 stretches the graph (including grap's estimate of the accompanying text) to be four inches wide; it is an alternative to altering the frame command. The macro blob is a plotting symbol that is much larger than bullet; the different name ensures that later references to bullet are unaffected. The troff commands within the blob string move the character down one-tenth of an em to center its plotting position (determined experimentally) and then reset the vertical position. The program produces this trivial (but large) graph.


## 4. Using Grap

Following are a few day-to-day matters about using grap.

### 4.1. Errors

Grap attempts to pinpoint input errors; for example, the input

```
.G1
i = i + 1
```

results in this message on stderr:

```
grap: syntax error near line 1, file -
    context is
            i = i >>> + <<< 1
```

The error was noticed at the + . Unfortunately, pinpointing is not the same as explaining: the real error is that the variable i was not initialized.

The "words" x and y are reserved (for the coord statement); you will get an equally inexplicable syntax error message if you use them as variable names. (This design is bad, but not nearly so bad as having the $\log$ and exp functions use base 10.)

Grap tries to load a file of standard macro definitions (/usr/lib/grap.defines) for terms like bullet, plus, etc. It doesn't complain if that file isn't found, but if you later use one of these words, you'll get a syntax error message.

Certain constructs suggested by analogy to pic do not work. For example, . GS and. GE would have been nicer than . G1 and . G2, but they were already taken. The pic construct

```
.PS <file
```

has been superseded by grap's copy command (which in turn has been retrofitted into pic).

### 4.2. Troff issues

You may use troff commands like .ps or .ft to change text sizes and fonts within a graph, or use balanced \s and $\backslash f$ commands within a string. Do not, however, add space (.sp) or change the line spacing (.vs, .ls) within a graph. Some defined terms like bullet contain embedded size changes; further qualifying them with grap size commands may not always work.

Because grap is built on top of pic, the following quote from the pic manual is relevant: 'There is a subtle problem with complicated equations inside pic pictures - they come out wrong if eqn has to leave extra vertical space for the equation. If your equation involves more than subscripts and superscripts, you must add to the beginning of each such equation the extra information space 0 ', This feature was illustrated in the graph of the United States population in Section 3.

### 4.3. Alternatives

Besides grap and your local draftsperson, what other choices are there?
The S system |reference(slanguage chambers) provides a host of tools for statistical analysis, but somewhat fewer tools than grap for producing document-quality graphs. S produces graphs on the screen of a DMD 5620 terminal much more quickly than grap (often in seconds rather than minutes), but it takes somewhat longer to learn (at least for us). If you expect to do a lot of interactive data analysis, then $S$ is probably the right tool for you. $S$ may be used to generate pic commands.

The standard UNIX program graph provides many of the basic features of grap, though with quite a bit less control over details, particularly text. It produces output only in the UNIX $\operatorname{plot}(5)$ language, which may be processed by a variety of filters for a variety of output devices.

The original UNIX typesetter graphics programs are pic and ideal; you may be able to do as well without using grap as an intermediary. In particular, ideal provides shading and clipping, which are useful in presentation-quality bar charts and the like, but are well beyond the capabilities of pic.

## 5. References

| reference_placement

## 6. Reference Manual

In the following, italic terms are syntactic categories, typewriter terms are literals, parenthesized constructs are optional, and ... indicates repetition. In most cases, the order of statements, constructs and attributes is immaterial.

```
grap program:
```

. G1 (width in inches)
grap statement
. G2
A width on the . G1 line overrides the computed width, as in pic.

```
grap statement:
    frame |label | coord |ticks | grid | plot | line | circle | draw | new | next
    | graph| numberlist | copy |for | if | sh | pic | assignment | print
```

The frame statement defines the frame that surrounds the graph:

```
frame:
    frame (ht expr) (wid expr) ((side) linedesc) ...
side :
    top | bot | left | right
linedesc:
    solid | invis | dotted (expr) | dashed (expr)
```

Height and width default to 2 and 3 inches; sides default to solid. If side is omitted, the linedesc applies to the entire frame. The optional expressions after dotted and dashed change the spacing exactly as in pic.

The label statement places a label on a specified side:

```
label:
    label side strlist ... shift
shift:
    left|right|up|down expr...
strlist :
        str...(rjust|ljust|above|below)...(size (\pm) expr)...
str:
    "..."
```

Lists of text strings are stacked vertically. In any context, string lists may contain clauses to adjust the position or change the point size. Each clause applies to the string preceding it and all following strings. Labels may also have a width attribute, to override grap's default computation.

Normally the coordinate system is defined by the data, with 7 percent extra on each side. (To change that to 5 percent, assign 0.05 to the grap variable margin, which is reset to 0.07 at each . G1 statement.) The coord statement defines an overriding system:
coord:

```
coord (name) (x expr,expr) (y expr,expr) (log x | log y | log log)
```

Coordinate systems can be named; ranges, logarithmic scaling, etc., are done separately for each.
The ticks statement places tick marks on one side of the frame:

```
ticks:
    ticks side (in | out (expr)) (shift) (tick-locations)
tick-locations:
    at (name) expr (str), expr (str), ...
    | from (name) expr to expr (by (op) expr) str
```

If no ticks are specified, they will be provided automatically; ticks off suppresses automatic ticks. The optional expression after in or out specifies the length of the ticks in inches. The optional name refers to a coordinate system. If str contains format specifiers like $\% \mathrm{f}$ or $\% \mathrm{~g}$, they are interpreted as by printf. If no str is supplied, the tick labels will be the values of the expressions.

If the by clause is omitted, steps are of size 1 . If the by expression is preceded by one of,,$+- *$ or $/$, the step is scaled by that operator, e.g., * 10 means that each step is 10 times the previous one.

The grid statement produces grid lines along (i.e., perpendicular to) the named side.

```
grid:
            grid side (linedesc) (shift) (tick-locations)
```

Grids are labeled by the same mechanism as ticks. It is possible to draw grids without ticks by placing the phrase ticks off after the side name and before the iterator.

Plot statements place text at a point:

```
plot:
        strlist at point
        plot expr(str) at point
point:
        (name) expr,expr
```

As in the label statement, the string list may contain position and size modifiers. The plot statement uses the optional format string as in C's print $f$ statement - it may contain a $\circ \mathrm{f}$ or $\% \mathrm{~g}$. The optional name refers to a coordinate system.

The line statement draws a line or arrow from here to there:
line :
(line | arrow) from point to point (linedesc)
The circle statement draws a circle:

```
circle:
circle at point(radius expr)
```

The radius is in inches; the default size is small.
The draw statement defines a sequence of lines:

```
draw:
draw (name) linedesc (str)
```

Subsequent data for the named sequence will be plotted as a line of the specified style, with the optional str plotted at each point. The next statement continues a sequence:
next:

```
next (name) at point (linedesc)
```

If a line description is specified, it overrides the default display mode for the line segment ending at point. The new statement starts a new sequence; it has the same format as the draw statement.

A line consisting of a set of numbers is treated as a family of points $x, y_{1}, y_{2}$, etc., to be plotted at the single $x$ value.

```
numberlist:
    number ...
```

If there is only one number it is treated as a $y$ value, and $x$ values of $1,2,3, \ldots$ are supplied automatically.
Grap provides arithmetic with the operators $+,-,^{\star}, /$, and ${ }^{\wedge}$. Variables may be assigned to; assignments are expressions. Built-in functions include log, exp (both base 10 - beware!), int (truncates towards zero), sin, $\cos$ (both use radians), atan2 (dy, dx), sqrt, min (two arguments only), max (ditto), and rand () (returns a real number random on $[0,1)$ ).

The for statement provides a modest looping facility:
for :

```
for var from expr to expr (by (op) expr) do { anything }
```

The string may contain internally balanced braces. Alternatively, any other character may appear immediately after the word do, and the string is terminated by the next occurrence of that character. The text anything (which may contain newlines) is repeated as var takes on values from exprl to expr2. As with tick iterators, the by clause is optional, and may proceed arithmetically or multiplicatively. In a for statement, the from may be replaced by " $=$ '".

The if-then-else statement provides conditional evaluation:

```
if:
```

if expr then \{ anything \} else \{ anything \}
The else clause is optional. Relational operators include $==,!=,>,>=,<,<=,!,| |$, and $\& \&$. Strings may be compared with the operators $==$ and $!=$.

It is possible to convert numeric expressions to formatted strings:

```
sprintf("format", expr, expr, ...)
```

is equivalent to a quoted string in any context. Variants of $\% \mathrm{f}$ and $\% \mathrm{~g}$ are the only sensible format conversions.
Grap provides the same macro processor that pic does:

```
define macro-name { anything }
```

Subsequent occurrences of the macro name will be replaced by the string, with arguments of the form $\$ n$ replaced by corresponding actual arguments. Macro definitions persist across . G2 boundaries, as do values of variables.

The copy statement is somewhat overloaded:
copy "filename"
includes the contents of the named file at that point;

```
copy "filename" thru macro-name
```

copies the file through the macro; and

```
copy thru macro-name
```

copies subsequent lines through the macro; each number or quoted string is treated as an argument. In each case, copying continues until end of file or the next .G2. The optional clause until str causes copying to terminate when a line whose first field is str occurs. In all cases, the macro can be specified inline rather than by name:

```
copy thru { macro body }
```

The sh command passes text through to the UNIX shell.

## sh:

sh \{ anything \}
The body of the command is scanned for macros. The built-in macro pid is a string consisting of the process identification number; it can be used to generate unique file names.

The pic command passes text through to pic with the "pic" removed; variables and macros are not evaluated. Lines beginning with a period (that are not numbers) are passed through literally, under the assumption that they are troff commands.

The graph statement
graph:
graph Picname (pic-text)
defines a new graph named Picname, resetting all coordinate systems. If any graph commands are used in a grap program, then the statement after the .G1 must be a graph command. The pic-text can be used to position this graph relative to previous graphs by referring to their Frames, as in

```
graph First
graph Second with .Frame.w at First.Frame.e + (0.1,0)
```

Macros and expressions in pic-text are not evaluated. Picnames must begin with a capital letter to satisfy pic syntax.
The print statement
print :

```
print (expr | str)
```

writes on stderr as grap processes its input; it is sometimes useful for debugging.
Many reserved words have synonyms, such as thru for through, tick for ticks, and bot for bottom.

The \# introduces a comment, which ends at the end of the line. Statements may be continued over several lines by preceding each newline with a backslash character. Multiple statements may appear on a single line separated by semicolons. Grap ignores any line that is entirely blank, including those processed by copy thru commands.

When grap is first executed it reads standard macro definitions from the file/usr/lib/grap. defines. The definitions include bullet, plus, box, star, dot, times, htick, vtick, square, and delta.


[^0]:    $\dagger$ Throughout this document we will show only the first five lines and the last line of data files; omitted lines are indicated by ' ...'".

